

What are they?

- A **Taylor series** generates a polynomial function that approximates a function $f(x)$ for values of x near a value c for which that function's value is known.

e.g., you could use a Taylor polynomial to find the sines of angles near $\frac{\pi}{2}$, given that we know $\sin(\frac{\pi}{2}) = 1$. In this case, $c = \frac{\pi}{2}$ and we say that this Taylor series is *centered* on $\frac{\pi}{2}$.

- ▶ A polynomial derived by simplifying the first n elements of a Taylor series is referred to as an ***n*th-degree Taylor polynomial**.
- A **Maclaurin series** is a Taylor series centered on 0, that is, $c = 0$.

Calculation

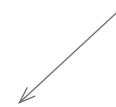
Taylor Series

$$F(x) = \sum_{n=0}^{\infty} \frac{f^{(n)}(c)}{n!} (x-c)^n$$

That is,

$$F(x) = f(c) + f'(c)(x-c) + \frac{1}{2}f''(c)(x-c)^2 + \frac{1}{6}f'''(c)(x-c)^3 + \dots$$

Note that the coefficients here are $1/0!, 1/1!, 1/2!, 1/3!, \text{etc.}$



Maclaurin Series

$$F(x) = \sum_{n=0}^{\infty} \frac{f^{(n)}(0)}{n!} (x^n)$$

That is,

$$F(x) = f(0) + f'(0)(x) + \frac{1}{2}f''(0)(x^2) + \frac{1}{6}f'''(0)(x^3) + \dots$$