

## Arithmetic Sequences

Each term is derived by adding a constant,  $d$ , to the previous term; *i.e.*,

$$a_n = a_{n-1} + d \quad \leftarrow \text{This is the recursive version of the sequence}$$

The  $n^{\text{th}}$  term of an arithmetic sequence:

$$a_n = a_1 + d(n - 1)$$

Note that  $n$  in this case is the number of elements you're adding, not necessarily the element number of the last element.

The sum of an arithmetic sequence with  $n$  terms:

$$S = \frac{n}{2}(a_{\text{first}} + a_{\text{final}})$$

### Finding $d$

$$d = a_2 - a_1$$

$$d = a_3 - a_2$$

etc.

## Geometric Sequences

Each term is derived by multiplying the previous term by a constant,  $r$ ; *i.e.*,

$$a_n = r \cdot a_{n-1} \quad \leftarrow \text{This is the recursive version of the sequence}$$

The  $n^{\text{th}}$  term of geometric sequence:

$$a_n = a_1 r^{n-1}$$

### Finding $r$

$$r = \frac{a_2}{a_1}$$

$$r = \frac{a_3}{a_2}$$

etc.

The sum of a geometric sequence with  $n$  terms:

$$S = a_{\text{first}} \left( \frac{1 - r^n}{1 - r} \right)$$

Note that  $n$  in this case is the number of elements you're adding, not necessarily the element number of the last

The sum of an infinite geometric sequence ( $-1 < r < 1$ )

$$S = \frac{a_1}{1 - r}$$

### Sigma Notation

$$\sum_{i=1}^6 3n - 6$$

The element number of the last element you are

The equation for calculating  $a_n$ .

The element number of the first element you are