

# Simple Harmonic Motion

## Basics

Angular speed,  $\omega = 2\pi f = 2\pi/T$

Period,  $T = 2\pi/\omega$

Frequency,  $f = 1/T = \omega/2\pi$

$x(t) = A\sin(\omega t)$

$v(t) = \omega A\cos(\omega t)$

$a(t) = -\omega^2 A\sin(\omega t)$

$= -\omega^2 x$  ← because  $x(t) = A\sin(\omega t)$

$v_{\max} = \omega A = 2\pi A f$

$a_{\max} = \omega^2 A$

## Springs

$F = -kx$

$\omega = \sqrt{k/m}$

$T = 2\pi\sqrt{m/k}$

$v^2 = \frac{k}{m}(A^2 - x^2)$

$a = \frac{kx}{m}$

## Potential Energy

Horizontal spring:  $U = \frac{1}{2}kx^2$

Vertical spring:  $U = \frac{1}{2}kx^2 + mgx$

Maximum PE:  $U_{\max} = \frac{1}{2}kA^2$

## Pendula (Pendulums?)

The following assumes that the angular displacement,  $\theta$ , of the pendulum is small enough that  $\sin(\theta) \sim \theta$ .

### Ideal Pendulum

$T = 2\pi\sqrt{\frac{L}{g}}$

### Physical Pendulum

$T = 2\pi\sqrt{\frac{I}{mgd}}$

$I$ , here, is moment of inertia

## Key to Symbols

**A** amplitude, m

**a** acceleration, m/s<sup>2</sup>

**f** frequency, Hz

**I** Moment of inertia

**k** spring constant, N/m

**L** pendulum length, m

**x, d** distance from rest, m

**T** Period, sec

**$\omega$**  angular velocity, rad/s